



# Investigation of a coaxial pulsed plasma thruster by electrothermal discharge in Teflon propellant

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## Abstract

The simplicity, efficiency, and reliability of pulsed plasma thrusters make them a preferred choice in low-power systems for microsatellites. In this paper, a coaxial electrothermal pulsed plasma thruster was designed and tested using Teflon as a solid propellant. The ablated mass was measured for different values of peak discharge current and number of pulses. The Experimental results of our system were compared with calculated values obtained using a 1-D time-dependent ETFLOW model for the electrothermal capillary system. The model was used to calculate the values of thrust and impulse for each case. Experimentally, increasing the number of pulses resulted in an increase in the total ablated mass and the capillary diameter. Experimentally, increasing the peak discharge current from 1.95 kA to 5.66 kA led to an increase in the ablated mass per pulse from 128.4  $\mu\text{g}$  to 980.8  $\mu\text{g}$  and the impulse from 340  $\mu\text{N}\cdot\text{s}$  to 2156  $\mu\text{N}\cdot\text{s}$ . In addition, extending the capillary length from 3 to 8 cm led to an increase in the ablated mass from 52  $\mu\text{g}$  to 326.2  $\mu\text{g}$ , consistent with the calculated data. Moreover, the thrust efficiency was investigated as a function of input energy and capillary length. The maximum achieved thrust efficiency was about 8.9% for an input energy of 6 J and a capillary length of 6 cm. Theoretically, the model predicted that thrust, impulse, and specific impulse increase with raising the peak discharge current.

**Keywords** PPT · Electrothermal discharge · Ablated mass · Thrust · Impulse · Specific impulse

## 1 Introduction

Worldwide interest in micro- and nano-satellites has been increasing due to their low cost and versatility, which make them suitable propulsion systems used in space exploration and interplanetary missions, such as station-keeping, maneuvering, and attitude control [1, 2]. Seeking advantages such as simplicity, stability, robustness, reliability, and low energy consumption, electric propulsion systems, especially Pulsed Plasma Thrusters (PPTs), have emerged as preferred alternative engines for small satellites rather than the chemical thrusters [3]. Although chemical thrusters can achieve higher thrust values, electric thrusters utilize less propellant, producing small thrust over a long duration [4]. In addition, PPTs work with variable thrust and specific impulse stages

and can provide small, discrete values of impulse [5, 6]. In contrast, PPTs suffer from some disadvantages, such as limited specific impulse and late-time ablation, which decreases the propellant utilization [7, 8].

Although Electrothermal PPTs (ETPPTs) suffer from low specific impulse [9], they emerged as high-thrust electric propulsion systems, achieving higher thrust levels than electromagnetic engines [10]. The thrust mechanism in ETPPTs depends on the thermal expansion of the generated plasma. The performance of many propellants; solid, liquid, and gas types has been tested. To achieve a high reliability and light weight system, solid propellants are preferred since they do not require a storage system and eliminate propellant leakage. Teflon is the most widely used solid propellant due to its ability to resist fire and corrosion, which make it suitable for high-temperature, long-duration operation [11]. In solid ablative ETPPTs, the energy stored in the capacitor bank is discharged between the two electrodes along the surface of the propellant, and due to temperature, a portion of the propellant is dissociated, ionized, then it forms plasma, which is accelerated by the pressure gradient, generating thrust.

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The performance of capillary ETPPTs is influenced by many factors, such as the capillary length, capillary diameter, and input voltage. Many studies were conducted on the capillary ET system to study its performance. T. Edamitsu and H. Tahara [12] investigated the performance of capillary-based ET thrusters with different values of capillary length in a range of 4 mm to 34 mm. It was shown that a longer cavity can achieve higher values of impulse, and this is in agreement with other researches [8] in which the mass shot per joule increases from 6.5  $\mu\text{g}/\text{J}$  to 11  $\mu\text{g}/\text{J}$  with increasing capillary length from 8 to 12 mm. In addition, increasing the input voltage will raise the value of ablated mass, impulse, and specific impulse. In contrast, increasing the capillary diameter from 3 to 5 mm, the mass shot per joule decreased from 6.5 to 4.2  $\mu\text{g}/\text{J}$ , which agrees with [13]. In addition, an endurance test was conducted by measuring the impulse values during 40,000 pulses. The impulse value decreases by increasing the number of shots [10]. Moreover, the impulse value was measured using a pendulum method where a small target was located close to the nozzle [4].

There are many models that have been developed to characterize the electrothermal designs. Keidar et al. developed a time-dependent model to study the electrothermal plasma thruster properties using a Teflon capillary [14]. Their model distinguished two layers between the inner Teflon wall and the arc plasma: the collision-dominated hydrodynamic layer and the kinetic Knudsen layer. The model underpredicted the experimental results of ablated mass by about 25%. However, the calculated ablated mass and impulse had the same behavior as measured, increasing for longer cavity length and decreasing for larger cavity diameter [15]. Similarly, Edamitsu et al. conducted an unsteady state simulation of electrothermal discharge with Teflon propellant, taking into consideration that the plasma is in local thermodynamic equilibrium and exhibits only single ionization [10]. Their model showed good agreement between their calculated and experimental ablated mass, although their impulse calculations were slightly higher than experimental results [10]. Also, Cambier et al. established a zero-dimensional model to characterize the discharge properties of a polyethylene capillary [16]. The model includes the effect of high-density

non-ideal plasma effects, and it assumes that the plasma is in LTE and the ablated mass is fully ionized. It was found that increasing voltage improved impulse and thrust, while longer capillaries led to a reduction in specific impulse [16].

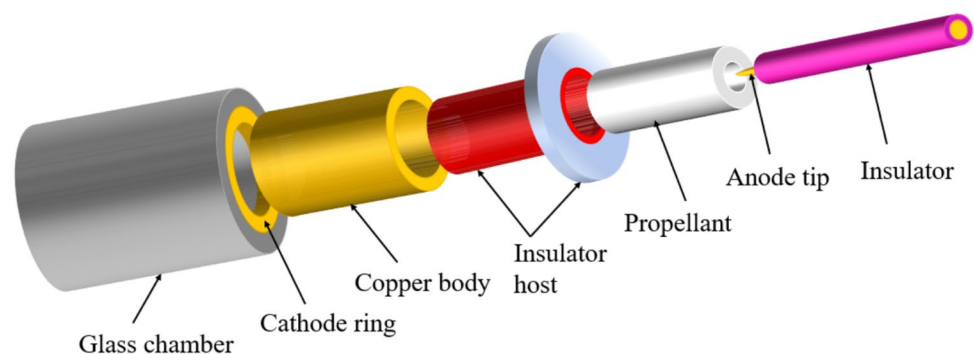
In this research, a capillary electrothermal PPT is constructed using a Teflon propellant of long tubes up to 6 cm. The ablated mass per pulse is measured with different peak currents. In addition, the ablated mass and impulse were measured as a function of the capillary length and diameter. The relationship between the number of pulses and ablated mass per pulse was measured during 5000 pulses. The experimental data were compared with calculated values obtained using ETFLOW modeling [17–22]. The model is used to study the variation of thrust with discharge time and to calculate various discharge parameters such as velocity, heat flux, plasma density, and pressure, as functions of capillary length and discharge current.

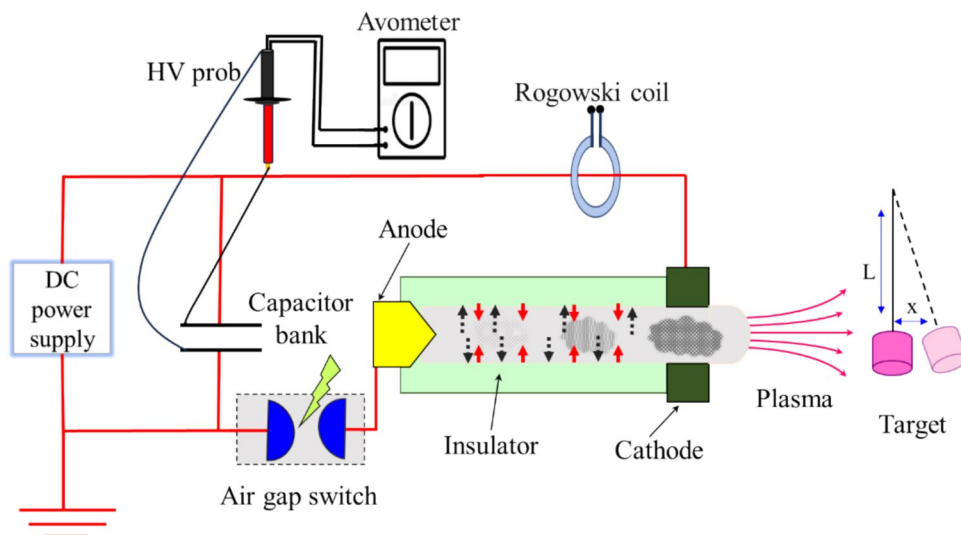
## 2 Experimental setup

Figure 1 shows a schematic diagram of the electrothermal capillary PPT system. It consists of a glass vacuum chamber of 27 cm in height and 23 cm in diameter and two electrodes, an annular ring cathode connected to an extended copper body with an inner diameter of 3 cm and a rod anode of 4 mm diameter, which is shielded by polyacrylic as an insulator, and an anode tip is 1 cm in long. Between the two electrodes, an insulating material with an inner diameter of 1.7 cm serves as a host for the propellant. The whole system is evacuated using a mechanical rotary pump.

Figure 2 illustrates the electric circuit to which the system is connected, while Table 1 presents the experimental parameters used in this study by varying the applied input. The circuit consists of a DC power supply, a capacitor bank with a total capacitance of 5.32  $\mu\text{F}$ , and an air gap switch. A Rogowski coil is connected to an integrator circuit and an oscilloscope to measure the discharge current. The used coil is 109 turns, with a major diameter of 4.5 cm, and an inner diameter of 4 mm for each turn. The coil is connected to an RC integrator circuit, and the charging voltage

**Fig. 1** The components of the electrothermal capillary system



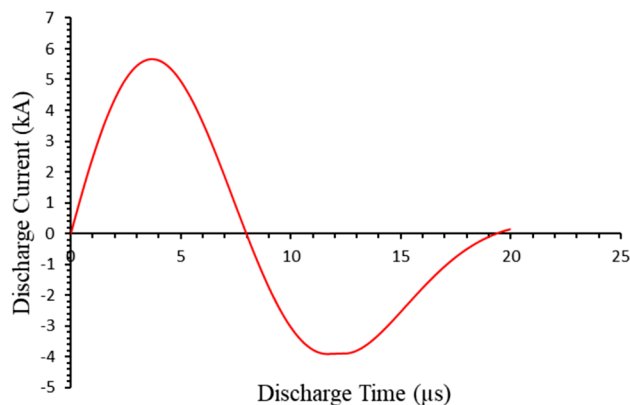
**Fig. 2** The electrical circuit connected to the system**Table 1** The circuit parameters used in discharge

Initial voltage (kV)	1.5–4
Discharge current (kA)	1.95–5.66
Pulse duration ( $\mu\text{s}$ )	19
Capacitance ( $\mu\text{F}$ )	5.32
Capillary length (cm)	5
Capillary diameter (mm)	4
Material of capillary	Teflon

is measured using a high-voltage probe. Besides, the impulse is measured using the pendulum method. A cylindrical target with a mass of 1 g is suspended by a string so that the mass is positioned in front of the nozzle. When plasma is expelled from the capillary, it pushes the target. By knowing the horizontal displacement of target and string length, the impulse could be calculated.

The system is a self-discharge one; capacitors discharge into the capillary through an air-gap switch, initiating an arc. The heat radiated from the discharge current via Joule heating is absorbed by the inner wall of the capillary propellant, causing ablation of the wall material [23, 24]. The dissociated atoms and molecules become ionized, forming high-density and high-pressure plasma inside the capillary. The plasma exits the capillary due to the high-pressure gradient, generating thrust. The amount of the ablated mass and the plasma exit velocity control the impulse generated by the thruster.

The ablated atoms from the walls form a dense vapor that can absorb part of the radiant energy and reduce the amount of energy that reaches the wall. Only a fraction of the heat flux is transmitted to the wall, and the arc is not assumed an ideal blackbody. Therefore, the ablated mass is affected by the value of the transmission heat factor (gray factor), which is less than

**Fig. 3** Waveform of discharge current with input voltage of 4kV

one for the non-ideal blackbody radiation. This phenomenon is called the vapor shielding effect [25, 26].

Figure 3 shows the wave signal of the discharge current for an input voltage of 4 kV. The discharge current peak was measured using a Rogowski coil connected to an integrator circuit. The discharge current reaches a peak of 5.66 kA at 3.66  $\mu\text{s}$ .

The next section addresses the effect of changing the applied voltage on the ablated mass and the effect of the capillary dimensions, such as length and diameter, on the values of ablated mass. The voltage was varied between 1.5 kV and 4 kV for a Teflon capillary of 5 cm long and 4 mm in diameter. The circuit's capacitance is 5.32  $\mu\text{F}$ , and the pulse duration is 19  $\mu\text{s}$ .

### 3 Theoretical considerations

The theoretical results were obtained using the ET FLOW modeling code, which provides a deep description of the essential physical parameters of the capillary Electrothermal system including, the plasma density, temperature, pressure, velocity, ablated mass, and internal energy. The model is based on several assumptions, which can be summarized as follows: the model is 1D, time-dependent. There is no effect due to the radial phase. Plasma is assumed to be in local thermodynamic equilibrium, and the ablated particles from the surface of the capillary partially absorb the incoming radiation. Only a fraction of heat flux reaches the wall. Ohmic heating is considered uniform in the capillary, while frictional forces and magnetic pressure are negligible, radiant heat transfer is dominant, and the capillary hollow radius remains constant [17, 18]. The basic equations to build this model include conservation of mass, momentum, and energy [19–21, 26], besides the thrust equations such as thrust, impulse, and specific impulse which can describe the thruster's performance.

The mass conservation equation indicates that the difference between the rate of ablation and the number density of particles which enter or leave the capillary is equal to the time rate of change of plasma density inside the capillary [17, 19–21]:

$$\frac{\partial n}{\partial t} = \dot{n} - \frac{\partial(vn)}{\partial z} \quad (1)$$

where  $n$  is the number density of the plasma ( $\text{m}^{-3}$ ),  $v$  is the plasma velocity ( $\text{m/s}$ ), and  $\dot{n}$  is the rate of ablation ( $\text{m}^{-3} \cdot \text{s}^{-1}$ ). The momentum conservation equation could be given as:

$$\frac{\partial v}{\partial t} = -K_{press} - K_{KE} - K_{dens} \quad (2)$$

where  $K_{press}$  is for pressure gradient,  $K_{KE}$  is the gradient of kinetic energy, and  $K_{dens}$  is for change in density due to the ablation process. Also, the energy conservation equation can be given as:

$$n \frac{\partial U}{\partial t} = U_{joule} - U_{Rad} - U_{work} - U_{trans} \quad (3)$$

where  $U_{joule}$  is for joule heating,  $U_{Rad}$  is thermal radiation,  $U_{work}$  is the work done by plasma, and  $U_{trans}$  is loss due to particles entering or leaving the capillary.

The thrust ( $\Gamma$ ) is the force responsible for propelling plasma. It is defined as the product of the mass flow rate multiplied by the exhaust velocity of plasma from the capillary end [27] and the impulse ( $I_m$ ) is obtained by integrating the thrust [27] over the time of the pulse duration [28]:

$$\Gamma = \frac{dm}{dt} \cdot v \quad (4)$$

$$I_m = \int \Gamma dt = v_{ex} \int_0^t \frac{dm}{dt} dt \quad (5)$$

The specific impulse  $I_s$  is defined as the impulse per unit weight of propellant [27], and given by:

$$I_s = \frac{\int \Gamma dt}{g \cdot \int_0^t \frac{dm}{dt} dt} \quad (6)$$

where:  $g$  is the acceleration due to gravity.

### 4 Results and discussion

The ablation rate could be described according to the energy of the radiation heat flux which is transferred to the capillary wall, causing material ablation. The rate of ablation  $\dot{n}$  is given by:

$$\dot{n} = \frac{2q}{RH_{sub}A_p} \quad (7)$$

where  $H_{sub}$  is the specific heat of sublimation ( $\text{J/kg}$ ),  $R$  is the capillary radius,  $A_p$  is the mass of the atom constitutes plasma ( $\text{kg/atom}$ ), and  $q$  is radiation heat flux ( $\text{W/m}^2$ ) [20, 21], which could be given by [17, 18]:

$$q = F_t \sigma_s (T^4 - T_{vap}^4) \quad (8)$$

where  $\sigma_s$  is Stefan – Boltzmann constant,  $T$  is plasma temperature,  $T_{vap}$  is the vaporization temperature of the capillary, and  $F_t$  is the energy transmission factor (gray factor) which for organic polymers such as Teflon and polyethylene can be given by [29]:

$$F_t = 1 - e^{-0.025(P_r)^{0.6}} \quad (9)$$

where:  $P$  is the pressure (in bar), and  $r$  is the arc radius (mm). It is assumed that the plasma fills all the capillary tubes, therefore  $r \approx R$ .

The radiation heat from the arc depends on the plasma temperature and transmission heat factor. For the ideal case, the transmission heat factor is equal to one, meaning that the radiation behaves as ideal blackbody radiation. However, because of the vapor-shielding effect caused by the ablated molecules, the transmission heat factor varies with the pressure inside the capillary and the arc radius. Increasing either the plasma temperature or transmission heat factor leads to a higher heat flux, thereby, enhancing the ablation process. In the next sections, we address various factors affecting the discharge and propulsion.

#### 4.1 Discharge current

Figure 4 shows the variation in ablated mass as a function of the peak discharge current. Experimentally, increasing the peak current from 1.95 kA to 5.66 kA results in an increase in the ablated mass from 128.4  $\mu\text{g}$  to 980.8  $\mu\text{g}$  per pulse following the equation  $M[\mu\text{g}] = 231.79 I[\text{kA}] - 370.93$ . A higher current leads to a rise in the temperature inside the capillary, which in turn increases the radiation heat flux on the inner surface of the capillary and thereby increases the ablated mass.

The calculated data using the ideal transmission heat factor  $F_t = 1$ , the mass increases with peak current from 285  $\mu\text{g}$  to 1170  $\mu\text{g}$ , which is greater than the experimental values. However, the calculated values using the transmission heat factor according to Eq. 9 show that the mass increases from 145  $\mu\text{g}$  to 797  $\mu\text{g}$ , which closely aligns with experimental data. The radiation from the arc is not purely ideal blackbody radiation because not all the radiation produced by the arc reaches the wall due to the vapor shielding effect, which is caused by dissociated atoms and molecules. This shielding prevents a part of the radiation from reaching the inner wall of the capillary, and allows only a fraction of incident radiation. As a result, the ideal transmission heat factor overestimates the ablated mass compared to the values measured experimentally.

Figure 5 shows the capillary diameter variation before and after 5000 pulses. Also, Fig. 6 shows the variation of total ablated mass and capillary diameter as a function of discharge pulses. Increasing the number of pulses increases the total ablated mass from 0.064 g after 500 pulses to 1.26 g after 5000 pulses, with an average ablated mass of 206.2  $\mu\text{g}$  per pulse. As a result of this ablation, the capillary diameter became wider and increased from 4 mm to 5.5 mm. By measuring the ablated mass after a specified number of pulses, and assuming a uniform ablation along the length,

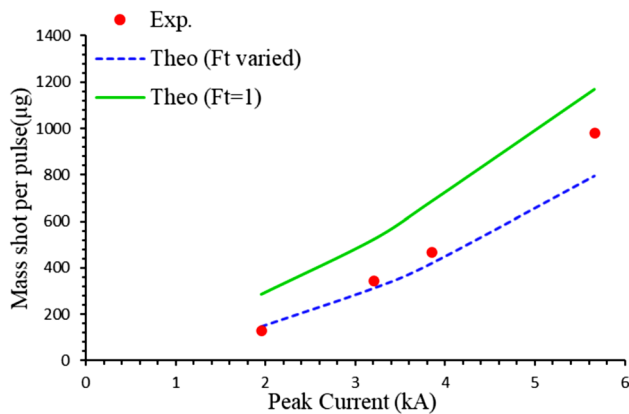


Fig. 4 Change in ablated mass with peak current

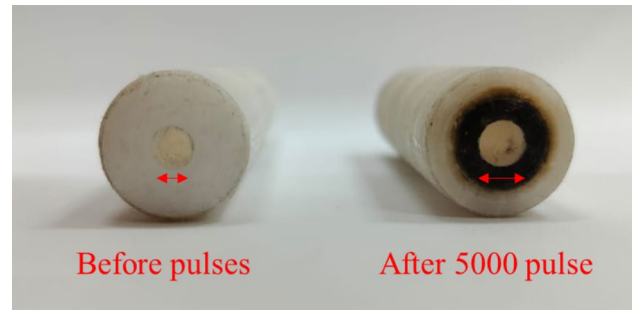


Fig. 5 The change in the capillary diameter due to the number of shots

the change in the capillary diameter as a function of the number of pulses can be calculated from the equations:

$$V = \frac{m}{\rho_t}, V = \frac{D^2}{4} \pi L \quad (10)$$

where  $D$  is the capillary diameter,  $\rho_t$  is the Teflon density (2.29  $\text{gm}/\text{cm}^3$ ) and  $L$  is the capillary length.

Figure 7 shows the change in the peak heat flux, plasma density, pressure, and exit velocity with peak current. As the peak current increases from 1.95 kA to 5.66 kA, the heat flux radiated from the arc increases from 0.63  $\text{GW}/\text{m}^2$  to 3.3  $\text{GW}/\text{m}^2$  following the power law  $Q[\text{GW}/\text{m}^2] = 0.22 I[\text{kA}]^{1.56}$ , as a result, the ablation of propellant increases accompanied by a rise in plasma density from 0.11  $\text{kg}/\text{m}^3$  to 0.62  $\text{kg}/\text{m}^3$  following the power law  $\rho [\text{kg}/\text{m}^3] = 0.039 I[\text{kA}]^{1.5814}$ . Increasing plasma density increases the pressure inside the capillary from 5.1 bar to 31 bar following the power law of  $P[\text{bar}] = 1.63 I[\text{kA}]^{1.69}$ . Also, the exit velocity increases from 2.85  $\text{km}/\text{s}$  to 3.15  $\text{km}/\text{s}$  following the scaling law  $v[\text{km}/\text{s}] = 0.078 I[\text{kA}] + 2.72$ . Increasing the input current leads to a rise in temperature inside the capillary which

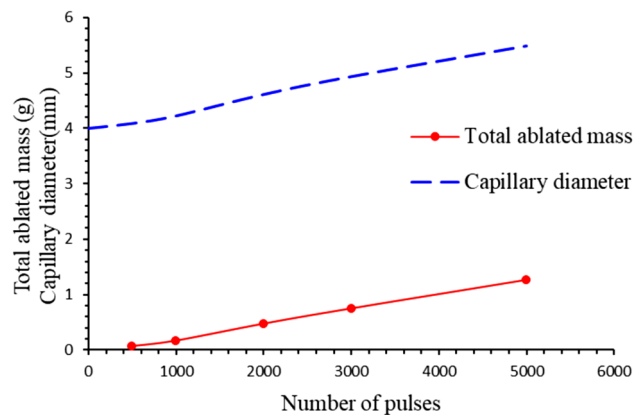
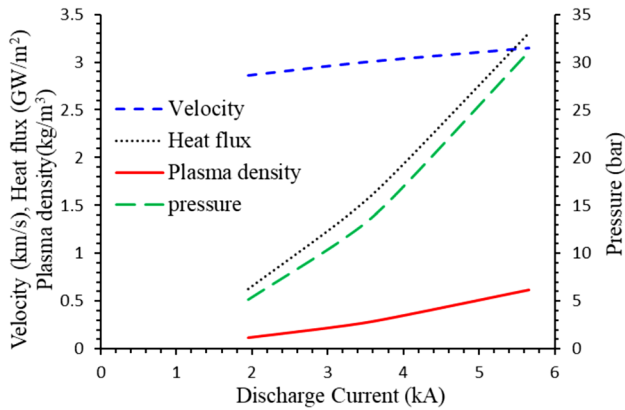


Fig. 6 The change in total ablated mass and capillary diameter with the number of shots

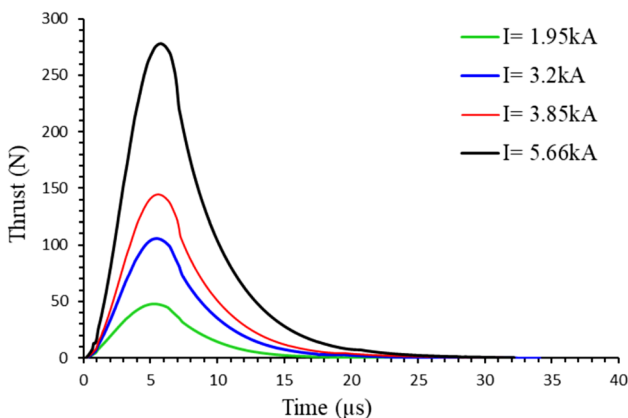


**Fig. 7** Increasing the peak of heat flux, plasma density, pressure, and exit velocity with increasing the peak current

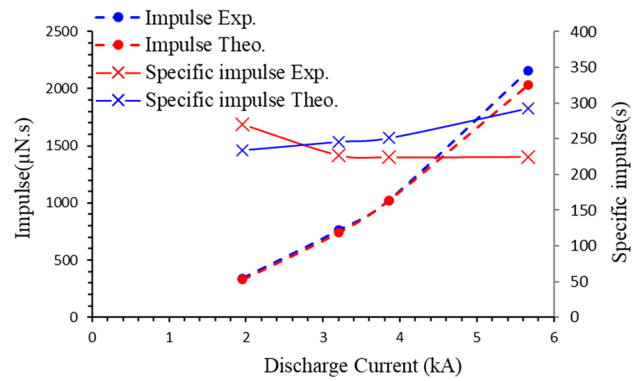
in turn increases the kinetic energy of plasma species, hence, the exit velocity increases.

It is shown that with increasing the number of pulses; the capillary diameter increases and the ablation rate tends to reduce as the capillary diameter increases with increasing the number of pulses. An increase in capillary diameter reduces the energy density, i.e., reduces the incident heat flux reaches the inner wall, which leads to decreases the ablation rate.

Figure 8 shows the change in calculated thrust profiles with different input voltages. The peak thrust increases from 47.6 N to 278 N by increasing as the discharge current peak rises from 1.95 kA to 5.66 kA. All curves reach the peak thrust simultaneously at 5.5  $\mu$ s and vanish by the end of discharge. Increasing the input current leads to a rise in the radiation heat flux from the arc, and this, according to Eq. 7, increases the ablation rate from the capillary and enhances the exit velocity. Consequently, the thrust values are increased, as shown in Eq. 4.



**Fig. 8** Thrust profile for different discharge current



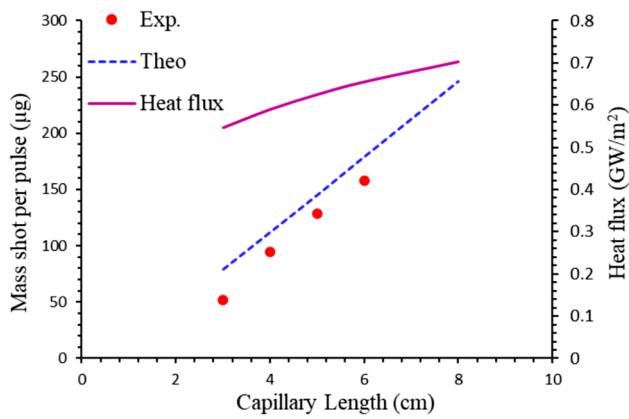
**Fig. 9** Change in measured and calculated impulse and specific impulse with discharge current

Figure 9 shows the change in measured and calculated impulse values, as well as the specific impulses as a function of the peak discharge current value. The impulse was measured experimentally using the pendulum method [4]. Experimentally, as the peak current increased from 1.95 kA to 5.66 kA, the impulse rises from 340  $\mu$ N.s to 2156  $\mu$ N.s [8, 10]. The specific impulse decreasing from 270 to 226s for discharge current of 3.2 kA, then increasing the current to about 5.66 kA does not significantly affect the values. Theoretically, the impulse increases from 330  $\mu$ N.s, which is in good agreement with experimental data, while the specific impulse increased from 234 s to 292.7 s [8, 10]. Increasing the discharge current peak enhances the ablation due to the temperature rise, which in turn increases the exit velocity of the plasma, according to the thrust equation Eq. 4. Thrust increases with both the ablated mass and exit velocity, which increases impulse as well, according to Eq. 5.

From the previous discussion, increasing the discharge current, results in a higher heat flux, and temperature incident on the inner wall of the capillary are also increased. As a result, the ablation process increased, accompanied by an increase in impulse. In addition, increasing the ablation process raises the plasma density inside the capillary; hence, the pressure is also increased. Moreover, as the temperature and pressure are rising inside the capillary, the kinetic energy of the plasma species also increases, which in turn increases velocity and impulse.

## 4.2 Capillary length

Figure 10 shows the change in the ablated mass and heat flux with capillary length for a peak discharge current of 1.95 kA using Eq. 9 for calculating the transmission heat factor, as it produces results in good agreement with experimental measurements. Experimentally, the ablated mass increases from 52  $\mu$ g to 158  $\mu$ g as the capillary length



**Fig. 10** The change in ablated mass as a function of capillary length

increased from 3 to 6 cm following the linear relation of  $M[\mu\text{g}] = 35.22 L[\text{cm}] - 50.34$ . The calculated data follows the same trend where the ablated mass increased from 79  $\mu\text{g}$  to 179  $\mu\text{g}$ . The heat flux also increases from 0.55  $\text{GW}/\text{m}^2$  to 0.66  $\text{GW}/\text{m}^2$  following the scaling law of  $Q\left[\frac{\text{GW}}{\text{m}^2}\right] = 0.16\ln(L[\text{cm}]) + 0.38$ . The longer capillaries have wider area exposed to radiation flux, which leading to higher ablation rates and greater ablated mass [8]. According to Eq. 8, the heat flux is proportional to the fourth power of the temperature, so it increases even with the slight increase of the temperature.

The plasma state is described by a modified Saha equation, which explains the relationship between the ionization potential and the effective charge state using the equation [26]:

$$I_i(Z_{\text{eff}} + 0.5) = K_B T \ln\left(\frac{AT^{1.5}}{Z_{\text{eff}} n}\right) \quad (11)$$

Hence  $I_i$  is the ionization potential and  $A$  is constant.

The pressure ( $P$ ) inside the capillary can be determined using the equation of state [17, 18]:

$$P = nK_B T(1 + Z_{\text{eff}}) \quad (12)$$

where  $Z_{\text{eff}}$  is the effective charge state which is given as [17, 18]:

$$Z_{\text{eff}} = \frac{\sum_j Z_j^2 n_j}{n_e} \quad (13)$$

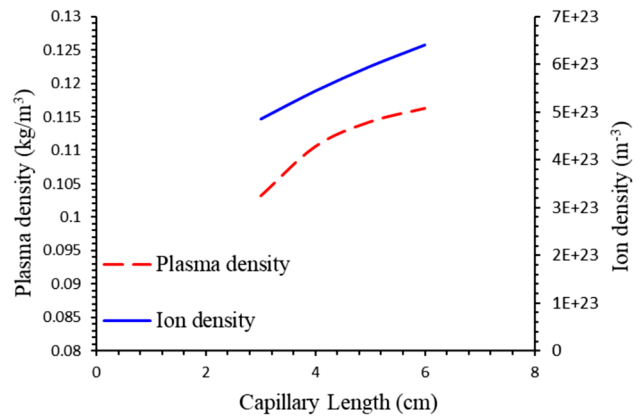
where  $j$  refers to the ion species of charge state  $z$ , and  $n_e$  is the density of electrons and the summation over the ions only.

The equations explain the effects of both the temperature and ion species on pressure, which in turn affects the ablation rate and the thrust properties. Increasing the

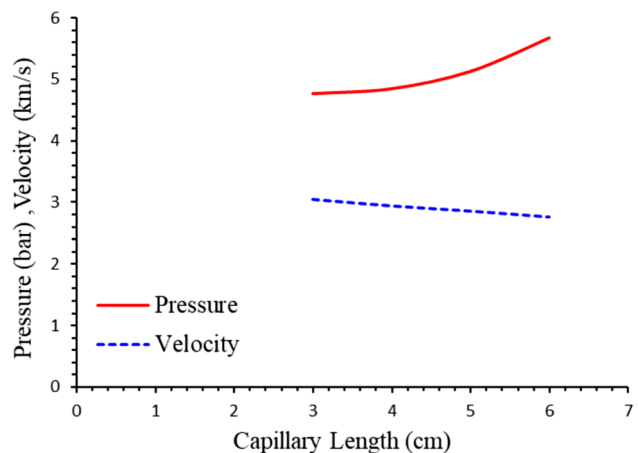
plasma temperature leads to a higher ionization of plasma species, consequently enhancing the ablation rate from the capillary wall. This rises the pressure inside the capillary, consequently increasing the thrust and impulse values.

Figure 11 shows the variation of plasma and ion number density as a function of the capillary length for a peak current of 1.95 kA. By increasing the capillary length from 3 to 6 cm, the ablation increases leading to a rise in plasma density from 0.1  $\text{kg}/\text{m}^3$  to 0.12  $\text{kg}/\text{m}^3$  and an increase in the ion number density from  $4.85 \times 10^{23} \text{ m}^{-3}$  to  $6.41 \times 10^{23} \text{ m}^{-3}$  following the power equation  $n_i [\text{m}^{-3}] = 3 \times 10^{23} L[\text{cm}]^{0.4011}$ . The increase in plasma and ion number density with capillary length is related to the greater area exposed to the heat, which enhances the ability of heat flux to ablate more layers from the inner capillary wall.

The variation of plasma exit velocity and pressure with the capillary length is illustrated in Fig. 12. According to Eq. 12, a rise in peak pressure accompanies the increase



**Fig. 11** Plasma density and ion density variation with the capillary length



**Fig. 12** The variation of pressure and velocity with the capillary length

in ion density. The peak pressure increases from 4.77 bar to 5.68 bar following the fitting equation  $P[\text{bar}] = 0.12 L[\text{cm}]^2 - 0.75 L[\text{cm}] + 5.97$ . On the other hand, extending the capillary length decreases the plasma exit velocity from 3 km/s to 2.8 km/s, following the linear equation  $v[\text{km/s}] = -0.094 L[\text{cm}] + 3.32$ . The reduction in velocity is related to the change in pressure according to Eq. 2, and is also affected by the higher ablated mass, which increases the drag force.

Figure 13 shows the variation of the thrust profile as a function of the capillary length. Increasing the capillary length from 3 to 6 cm increases the peak thrust per pulse from 33.3 N to 53N, taking into account that all curves have the same pulse width. Thrust begins to increase with the ablation process until it reaches its maximum value, after which it gradually decreases and vanishes by the end of the discharge. Increasing capillary length enhances the ablation rate and ion number density, causing a rise in thrust values according to Eq. 4 [16].

Figure 14 shows the change in measured and calculated impulse as a function of capillary length. By increasing the capillary length from 3 to 6 cm, the ablation rate increases due to the larger area exposed to heat. As a result, the measured impulse increases from 173  $\mu\text{N}\cdot\text{s}$  to 464.5  $\mu\text{N}\cdot\text{s}$  following the linear equation of  $I_m [\mu\text{N}\cdot\text{s}] = 80.1 L[\text{cm}] - 67.2$ , which is in good agreement with calculated values in which the impulse increased from 202  $\mu\text{N}\cdot\text{s}$  to 480  $\mu\text{N}\cdot\text{s}$ . In contrast, increasing the capillary length reduces the plasma velocity due to the change in pressure as given in Eq. 2. Thus, the measured specific impulse decreases from 339 to 265 s following the same trend with calculated

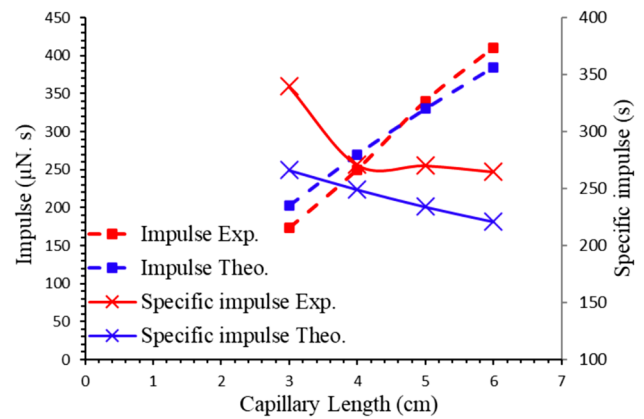


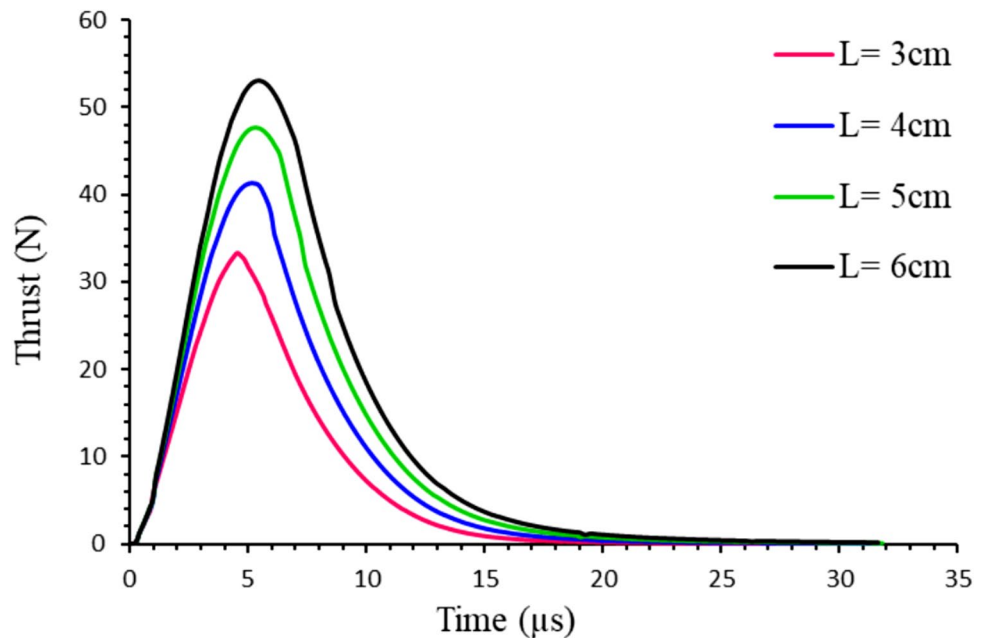
Fig. 14 Change in measured and calculated impulse, and specific impulse with the capillary length

values in which specific impulse drops from 266 to 212 s following the equation  $I_s[\text{s}] = -15.03 L[\text{cm}] + 310.2$ .

### 4.3 Capillary radius

Table 2 contains the values of ablated mass of two capillary diameters 4 mm and 6 mm with a fixed length for the capillary of 5 cm and with a discharge current of 1.95kA. The tables addresses the difference of several quantities, such as ablated mass, temperature, heat flux, peak pressure, peak velocity, plasma density, ion density, thrust, impulse, and specific impulse. As the capillary diameter increases from 4 to 6 mm, the capillary volume increases which causes a reduction in energy density reaching the wall leading by a reduction in the temperature from 1.81 eV to 1.57 eV.

Fig. 13 Thrust profile with different values of capillary length



**Table 2** Thrust parameters for different capillary diameters

Diameter (mm)	4 mm	6 mm
Ablated mass experimentally ( $\mu\text{g}$ )	128.4	85.2
Ablated mass theoretically ( $\mu\text{g}$ )	145	86
Impulse experimentally ( $\mu\text{N}\cdot\text{s}$ )	340	206
Impulse theoretically ( $\mu\text{N}\cdot\text{s}$ )	330	187.6
Specific impulse experimentally (s)	270	241.7
Specific impulse theoretically (s)	234	223
Peak temperature (eV)	1.81	1.57
Heat flux ( $\text{GW}/\text{m}^2$ )	0.63	0.24
plasma density ( $\text{kg}/\text{m}^3$ )	0.11	0.03
Ion density $\times 10^{23}$ ( $\text{m}^{-3}$ )	5.96	1.66
Peak pressure (bar)	5.13	1.27
Peak velocity (km/s)	2.86	2.7
Thrust (N)	47.6	25.8

According to Eq. 8, the heat flux follows the behavior of temperature, and it also decreases from  $0.63 \text{ GW}/\text{m}^2$  to  $0.24 \text{ GW}/\text{m}^2$ . According to Eq. 7, the ablated mass decreases with the reduction in heat flux, so it decreases experimentally from  $128.4 \mu\text{g}$  to  $85.2 \mu\text{g}$  accompanied by decreasing in impulse value from  $340 \mu\text{N}\cdot\text{s}$  to  $206 \mu\text{N}\cdot\text{s}$ .

The reduction in temperature and ablated mass is accompanied by a decrease in ion density and plasma density, consequently reducing the exit pressure as described by Eq. 12. Furthermore, the reduction in temperature reduces the kinetic energy of plasma species, results in a reduction of the exit velocity and, consequently, the thrust, impulse, and specific impulse [8, 12].

According to the previous discussions, as the capillary length increases, the ablation process also increases due to the larger surface area exposed to the radiation heat flux, which in turn leads to an increase in the plasma density, the pressure, and the impulse. In contrast, a reduction in specific impulse is observed due to a decrease in plasma velocity. On the other hand, increasing the capillary radius leads to a reduction in ablated mass and impulse due to the lower heat flux that is incident on the inner wall of the capillary.

#### 4.4 Thrust efficiency

Thrust efficiency is defined as the ratio of the kinetic energy gained and the input energy, as expressed by the following equation [30, 31]:

$$\eta = \frac{\frac{1}{2}mv^2}{E_{in}} = \frac{I_m^2}{2mE_{in}} \quad (14)$$

Table 3 shows thrust efficiency as a function of input energy and capillary length. It is shown that, at constant input energy of 6 J, thrust efficiency increases from 4.8 to

**Table 3** Thrust efficiency for different values of the input energy and the capillary length

Input energy (J)	Length (cm)	Ablated mass ( $\mu\text{g}$ )	Impulse ( $\mu\text{N}\cdot\text{s}$ )	Thrust efficiency %
6	3	52	173	4.8
6	4	94.2	250	5.5
6	5	128.4	340	7.5
6	6	158	410	8.9
10.6	5	342.6	761.4	7.9
23.9	5	465.8	1021.8	4.7
42.6	5	980.8	2156	5.6

8.9% with increasing capillary length from 3 to 6 cm, while for a capillary length of 5 cm, the thrust efficiency is varied between 7.5% and 4.7% as the input energy changed between 6 J and 42.6 J.

## 5 Conclusion

An electrothermal PPT experiment was designed with a Teflon capillary. The ablated mass of the propellant was measured for different values of the peak discharge current. By increasing the peak current from 1.95 kA to 5.66 kA, the ablated mass increased from  $128.4 \mu\text{g}$  to  $980.8 \mu\text{g}$  per pulse. In addition, the measured impulse increases from  $340 \mu\text{N}\cdot\text{s}$  to  $2156 \mu\text{N}\cdot\text{s}$ . Moreover, it was shown that increasing the number of pulses with a current of 1.95 kA, led to an increase in the total ablated mass from 0.064 g after 500 pulses to 1.26 g after 5000 pulses, and the capillary diameter increased from 4 to 5.5 mm. For 1.95 kA, increasing the capillary length from 3 to 6 cm raises the measured ablated mass from  $52 \mu\text{g}$  to  $158 \mu\text{g}$ , the measured impulse from  $173 \mu\text{N}\cdot\text{s}$  to  $464.5 \mu\text{N}\cdot\text{s}$ , and the measured specific impulse decreases from 339 to 265 s.

The experimental data were compared to calculated data obtained from the ETFLOW model, which describes electrothermal discharge based on fundamental equations, including the continuity equation, momentum equation, and velocity equation. The ablated mass was calculated using the ideal transmission heat factor and the modified one. The results from the modified transmission heat factor equation are more reliable as compared to the experimental results. Also, for a discharge current of 1.95 kA, the calculated ablated mass increased from  $79 \mu\text{g}$  to  $179 \mu\text{g}$ , and the impulse increased from  $202 \mu\text{N}\cdot\text{s}$  to  $480 \mu\text{N}\cdot\text{s}$  by increasing the capillary length from 3 to 6 cm, which agrees with the measured values, while the thrust efficiency increases from 4.8 to 8.9%.

Several discharge properties, such as velocity, heat flux, plasma temperature, and pressure, were analyzed and found

to increase with increasing peak current. In addition, thruster parameters such as thrust, impulse, and specific impulse were also studied as a function of peak current. It was found that, by increasing the peak discharge current from 1.95 to 5.66 kA, the measured impulse increased from 340  $\mu\text{N}\cdot\text{s}$  to 2156  $\mu\text{N}\cdot\text{s}$ . In contrast, the thrust efficiency is varied in the range between 7.5 and 4.7% as the input energy changed between 6 J and 42.6 J.

**Author contributions** M. M. Abo El-Hadeed Conducted the experiment, discussed the results, Writing, Data Curing, Formatting, and Review. M. E. Abdelkader Conducted the experiment, Discussed the results, Writing and Review. F. B. Diab Conducted the experiment, Discussed the results, Writing and Review. M. A. Abd Al-Halim Conducted the experiment, Discussed the results, Writing, Data Curing, Formatting, and Review. All authors read and approved the final manuscript.

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**Data availability** No datasets were generated or analysed during the current study.

## Declarations

**Conflict of interest** The authors declare no competing interests.

**Ethical approval** The study was conducted according to the guidelines of the Declaration of Benha University and approved by the Ethics Committee of the Faculty of Science, Benha University (Code: BUFS-REC-2024-247Phy).

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